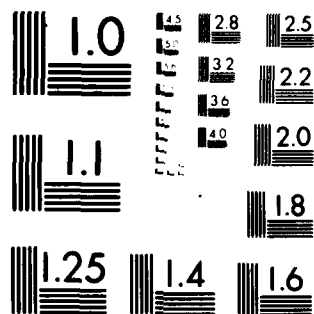AD-A098 425   ROCKWELL INTERNATIONAL THOUSAND OAKS CA SCIENCE CENTER   F/G 11/2
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TRANSFORMATION TOUGHENING

PART 5: EFFECT OF TEMPERATURE AND ALLOY ON FRACTURE TOUGHNESS

MAR. 81

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ABSTRACT

The critical stress intensity facor (K_c) of materials containing tetragonal ZrO_2 was found to decrease with increasing temperature and CeO_2 alloying additions, as predicted by theory. The temperature dependence of K_c was related to the temperature dependence of the chemical free energy change associated with the tetragonal $\rightarrow$ monoclinic transformation. Good agreement with thermodynamic data available for pure ZrO_2 was obtained when the size of the transformation zone associated with the crack was equated to the size of the ZrO_2 grains. The K_c vs CeO_2 addition data was used to estimate the tetragonal, monoclinic, cubic eutectoid temperature of 270°C in the ZrO_2-CeO_2 binary system.

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The critical stress intensity factor (K_c) of materials containing tetragonal ZrO_2 was found to decrease with increasing temperature and CeO_2 alloying additions, as predicted by theory. The temperature dependence of K_c was related to the temperature dependence of the chemical free energy change associated with the tetragonal ⇄ monoclinic transformation. Good agreement with thermodynamic data available for pure ZrO_2 was obtained when the size of the transformation zone associated with the crack was equated to the size

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of the ZrO_2 grains. The K_c vs CeO_2 addition data was used to estimate the tetragonal, monoclinic, cubic eutectoid temperature of 270°C in the ZrO_2-CeO_2 binary system.

1.0 INTRODUCTION

In Part 2,[1] theory was presented showing that the contribution to fracture toughness (K_c) by a stress-induced transformation is proportional to the chemical free energy change ($|\Delta G^C|$) associated with the transformation. For the ZrO_2 (tetragonal) $\rightarrow ZrO_2$ (monoclinic) transformation, $|\Delta G^C|$ is known to decrease with increasing temperature and with alloying ZrO_2 with Y_2O_3, CeO_2 etc. In this part of the series, experiments were designed to measure K_c as a function of temperature and alloy content. The temperaure dependence of K_c was measured on polycrystalline ZrO_2 and two-phase Al_2O_3/ZrO_2 materials in which 2 m/o Y_2O_3 was alloyed with the ZrO_2. The fabrication conditions and general properties of these materials have been reported in Part 4.[2]

A series of Al_2O_3/ZrO_2 materials in which CeO_2 was alloyed with the ZrO_2 phase was used to determine the effect of alloy content on K_c. As shown in Fig. 1, CeO_2 was a good candidate for this study since it forms an extensive solid-solution, tetragonal ZrO_2 phase field and lowers the tetragonal $\rightarrow$ monoclinic transformation temperature to < 25°C at ~ 20 m/o CeO_2.* Initial ZrO_2-CeO_2 sintering studies were not successful, i.e., higher CeO_2 contents (added to ZrO_2 powder as a soluable nitrate) resulted in a low density material. Hot-pressing was avoided, since CeO_2 reduces to Ce_2O_3 in environments produced by graphite dies. Attempts to sinter $Al_2O_3/30$ v/o ZrO_2 composite powders containing CeO_2 were successful in terms of density and phase content. Thus, these

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*In contrast, the working tetragonal phase field with Y_2O_3 additions is limited to compositions between 2 and 3 m/o Y_2O_3 in both single phase tetragonal ZrO_2[3] and Al_2O_3/ZrO_2 compositions.[2]
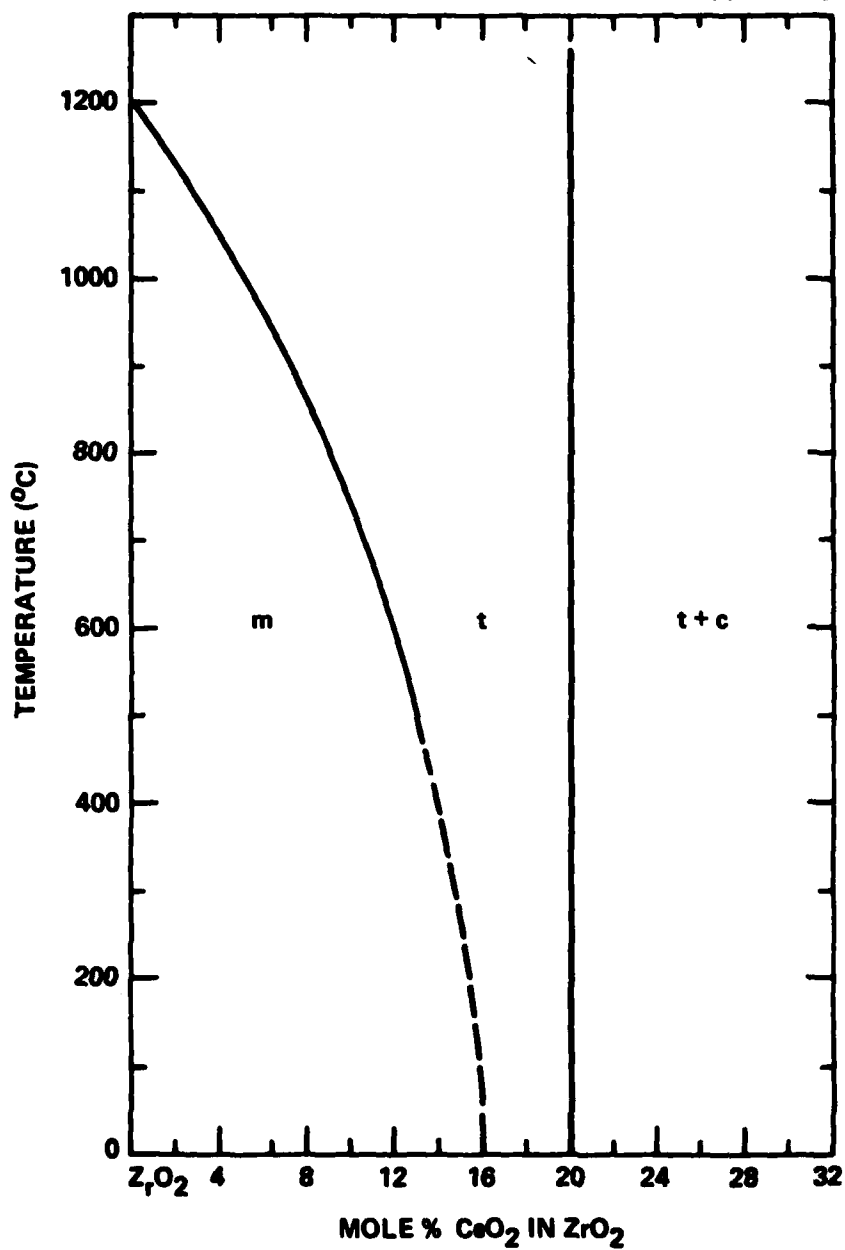
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Fig. 1   A portion of the ZrO_2-CeO_2 phase diagram.[5]

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composite materials were chosen for the fracture toughness vs alloying content
studies.

2.0 EXPERIMENTAL

2.1 Temperature Dependence

Four materials were chosen for this study. Three of these were hot-
pressed as detailed in Part 4:[2] $Al_2O_3/29.5$ v/o ZrO_2 (+2 m/o Y_2O_3), $Al_2O_3/45$ v/o
ZrO_2 (+2 m/o Y_2O_3) and ZrO_2 (+2 m/o Y_2O_3). The fourth material was a $Al_2O_3/30$
v/o ZrO_2 (+2 m/o Y_2O_3) composite sintered to 97% of theoretical density in air
at 1600°C/1 hr in which ZrO_2 was retained in its tetragonal state. The compos-
ite powders were prepared for sintering by mixing the required weight fractions
of Al_2O_3,* ZrO_2** and yttrium nitrade*** by ball milling in methanol (Al_2O_3
balls and plastic bottle), drying, calcining at 500°C/4 hrs, and isostatic
pressing at 350 MPa. Small bar specimens cut from each material were polished
in preparation for K_c measurements.

The indentation technique, developed by Evans and Charles,[4] was used to
measure K_c over the range of -196°C (liquid nitrogen) to 700°C. A Vickers
diamond indentor mounted in tungsten carbide was used with the device which
maintained a constant specimen temperature within the range noted. The device
consisted of an internally heated copper post, mounted within a metal flask.
The flask was attached to an x-y stage used to translate the specimen relative

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*Lindy B, Union Carbide Corp.
**Zircar, Corp.
***Research Chemicals Corp.

to the indentor. The stage was mounted on top of a local cell and was insulated from the flask with a machinable ceramic. The specimen was spring-clip loaded in a copper well attached to the post. A chromel-alumel thermocouple, spring-clip loaded to the external face of the specimen, was used to record temperatures. For the K_c measurements at temperatures < 25°C, the flask was externally insulated and filled with liquid nitrogen. The nitrogen was allowed to slowly evaporate to achieve the desired specimen temperature. For measurements at higher temperatures, the flask was filled with insulating ceramic fiber, and the internal heater was controlled to achieve the desired temperature. Argon was forced into the metal flask to protect the copper parts and diamond from oxidation. Between measurements the indentor was held just above the specimen to avoid a large temperature differential when the indentor was again forced into the specimen at 20 Kgms. A single specimen was used for the complete temperature range investigated; two measurements were made at each temperatures.

Flexural strengh measurements were made with one of the hot-pressed materials $\left[Al_2O_3/29.5 \text{ v/o } ZrO_2 \text{ (+2 m/o } Y_2O_3)\right]$ over the temperature range in which K_c measurements were made. Bar specimens (0.3 × 0.6 × > 3.0 cm) were diamond cut and ground and then annealed at 1300°C for 24 hr to eliminate the surface compressive stresses developed due to the transformation of surface material during grinding.[2] Three strength measurements were made in liquid nitrogen, a mixture of dry ice and methanol, room temperature and in air at higher temperatures.

2.3   Effect of Alloying

As indicated above, a series of Al_2O_3/30 v/o ZrO_2 composite materials in which CeO_2 was incorporated were found suitable for fracture toughness vs alloying content studies. Composite powders containing the appropriate weight fractions of Al_2O_3,* ZrO_2** and CeO_2*** were mixed and milled together in plastic bottles containing methanol and Al_2O_3 mill balls, dried by flash evaporation, calcined at 500°C/16 hr, isostatically pressed into plates and sintered at 1600°C/1 hr. Sixteen compositions containing a CeO_2 content between 6 to 22 m/o CeO_2 were fabricated. Densities of these composites ranged between 94% and 98% of theoretical, based on the density of tetragonal ZrO_2 calculated using the lattice parameter of a = 5.126 A and c = 5.224 A reported by Duwez and Odell.[5] X-ray diffraction analysis of the sintered surfaces showed that 100% of the ZrO_2 was retained in its tetragonal structure for compositions containing > 12 m/o CeO_2. Trace amounts of cubic ZrO_2 were observed for compositions containing 21 and 22 m/o CeO_2, consistent with previous phase equilibria studies.[5] Increasing amounts of monoclinic ZrO_2 were observed as the CeO_2 content decreased from 11 m/o to 6 m/o. Based on these observations, composites containing > 11 m/o CeO_2 were cut and polished for fracture toughness measurements at room temperature as described above.

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*Lindy B, Union Carbide Corp.
**Sub-micron ZrO_2, Zircar Corp.
***Added as Cerrium Nitrate, Research Chemicals Corp.

3.0 RESULTS

3.1 <u>Temperature Dependence</u>

Figure 2 illustrates that the fracture toughness decreases with increasing temperature for the four materials investigated. High, low and average values of K_c are defined by the scatter bar at each temperature. These data were fit to a linear equation:

$$K_c = A - mT \quad , \tag{1}$$

where T is temperature in degrees centigrade and the constants A and m are given in Table 1.

Table 1

Constants Defining Temperature Dependence of K_c

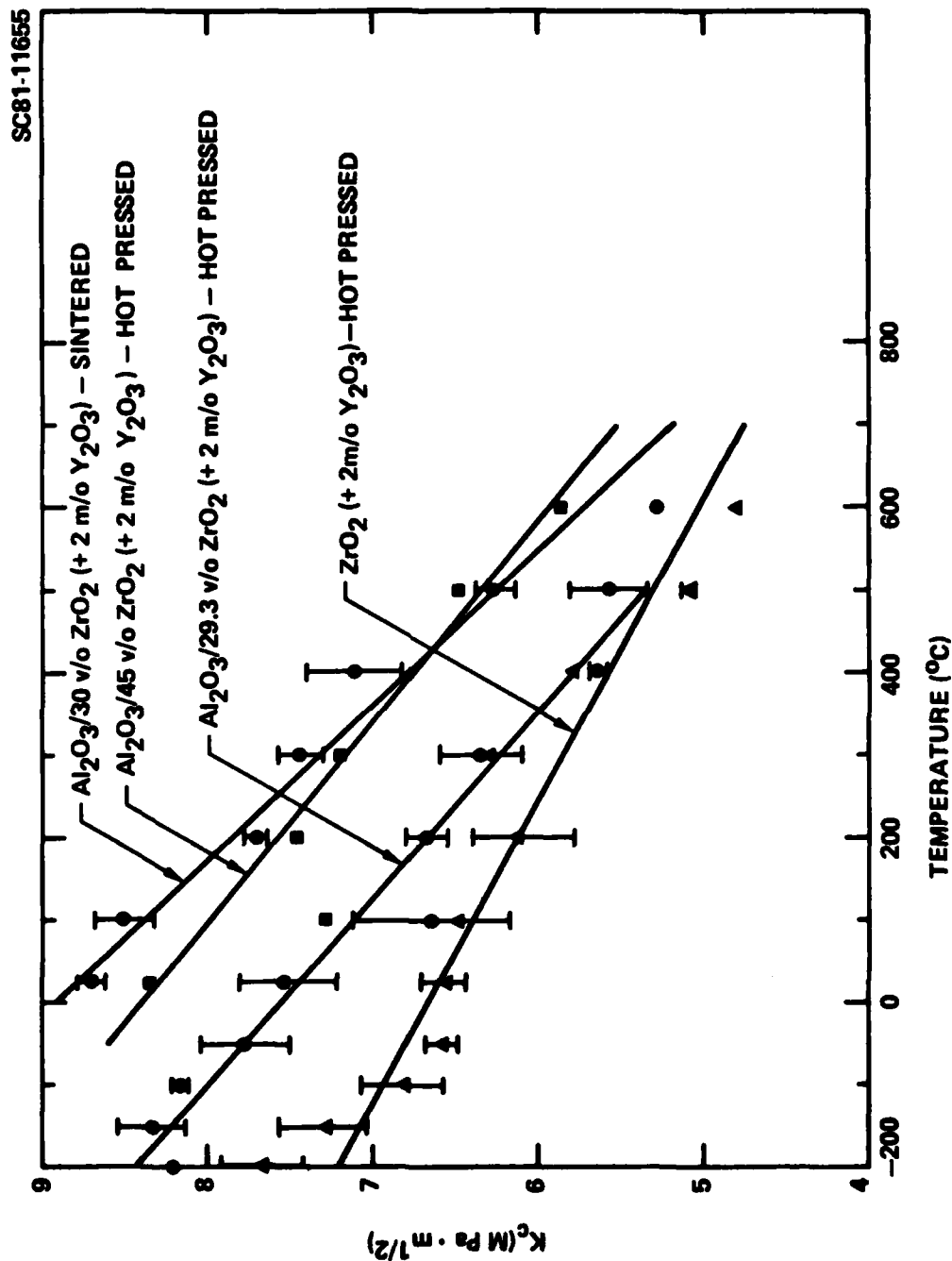| Material	Fabrication Conditions	A $(MPa \cdot m^{1/2})$	m $(MPa \cdot m^{1/2} \, C^{\circ -1})$	Correlation Coefficient
$Al_2O_3/29.3$ v/o ZrO_2 (+2 m/o Y_2O_3)	Hot-Pressed 1600°C/1 hr	7.56	0.0044	0.95
$Al_2O_3/45$ v/o ZrO_2 (+2 m/o Y_2O_3)	Hot-Pressed 1600°C/1 hr	6.78	0.0029	0.92
ZrO_2 (+2 m/o Y_2O_3)	Hot-Pressed 1600°C/1 hr	8.40	0.0041	0.99*
$Al_2O_3/30$ v/o ZrO_2 (+2 m/o Y_2O_3)	Sintered 1600°C/1 hr	9.96	0.0054	0.97

*Data at 100°C excluded.

Fig. 2 Critical stress intensity factor vs temperature for the four materials investigated.

The flexural strength data for the $Al_2O_3/29.3$ v/o ZrO_2 (+2 m/o Y_2O_3) composites are shown in Fig. 3. These data show that strength decreases with increasing temperature. The dashed line illustrates the expected temperature behavior of strength, based on the temperature behavior of K_c as reported in Table 1 for this composition and normalizing all data to the room temperature value.

3.2   Effect of Alloying

Figure 4 reports the K_c data vs the CeO_2 addition to the ZrO_2 in the $Al_2O_3/30$ v/o ZrO_2 sintered materials. Data obtained for the composition containing 11 m/o CeO_2 is low due to its substantial ($\sim$ 30 %) monoclinic ZrO_2 content. Over the range where only the tetragonal ZrO_2 phase is observed (12-20 m/o CeO_2), K_c decreases with increasing CeO_2 content. K_c appears to level off to $\sim$ 6 MPa$\cdot$m$^{1/2}$ at the reported tetragonal/cubic phase boundary (compositions containing > 20 m/o CeO_2). A linear relation was assumed over the range of 12-20 m/o CeO_2, resulting in the relation:

$$K_c = (10.32 - 0.202 \text{ M}) \text{ MPa} \cdot m^{1/2} \quad , \qquad\qquad (2)$$

where M = mole% CeO_2.

4.0 DISCUSSION

In Part 2[1] of this series, it was shown that the fracture toughness of a brittle material containing a phase which would undergo a stress-induced
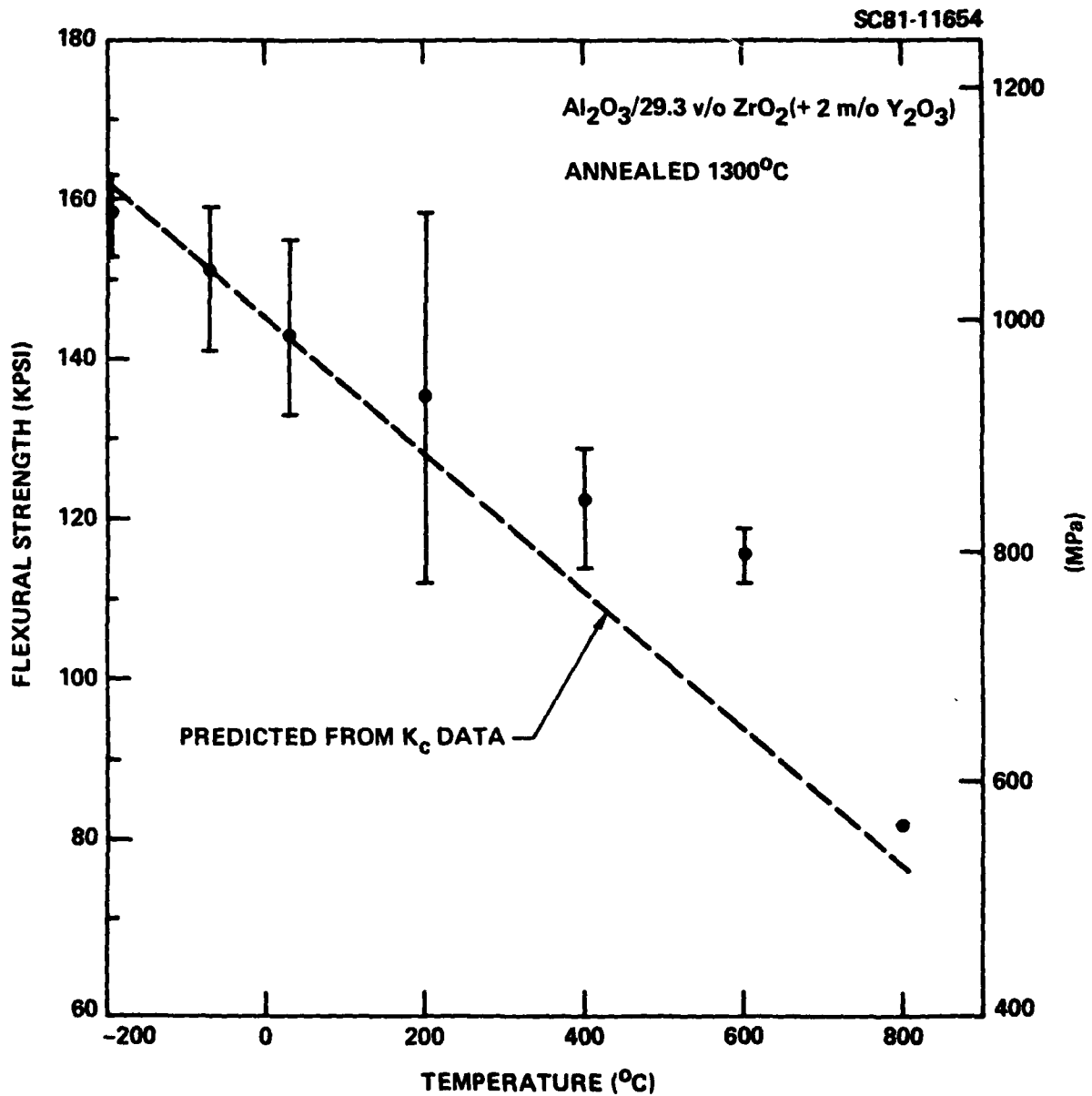
Fig. 3 Flexural strength vs temperature for the $Al_2O_3/29.3$ v/o ZrO_2 (+2 m/o Y_2O_3) material. Specimens first annealed at 1300°C/24 hrs.

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$Al_2O_3/30 \text{ V/o } ZrO_2 (+ CeO_2)$

ROOM TEMPERATURE

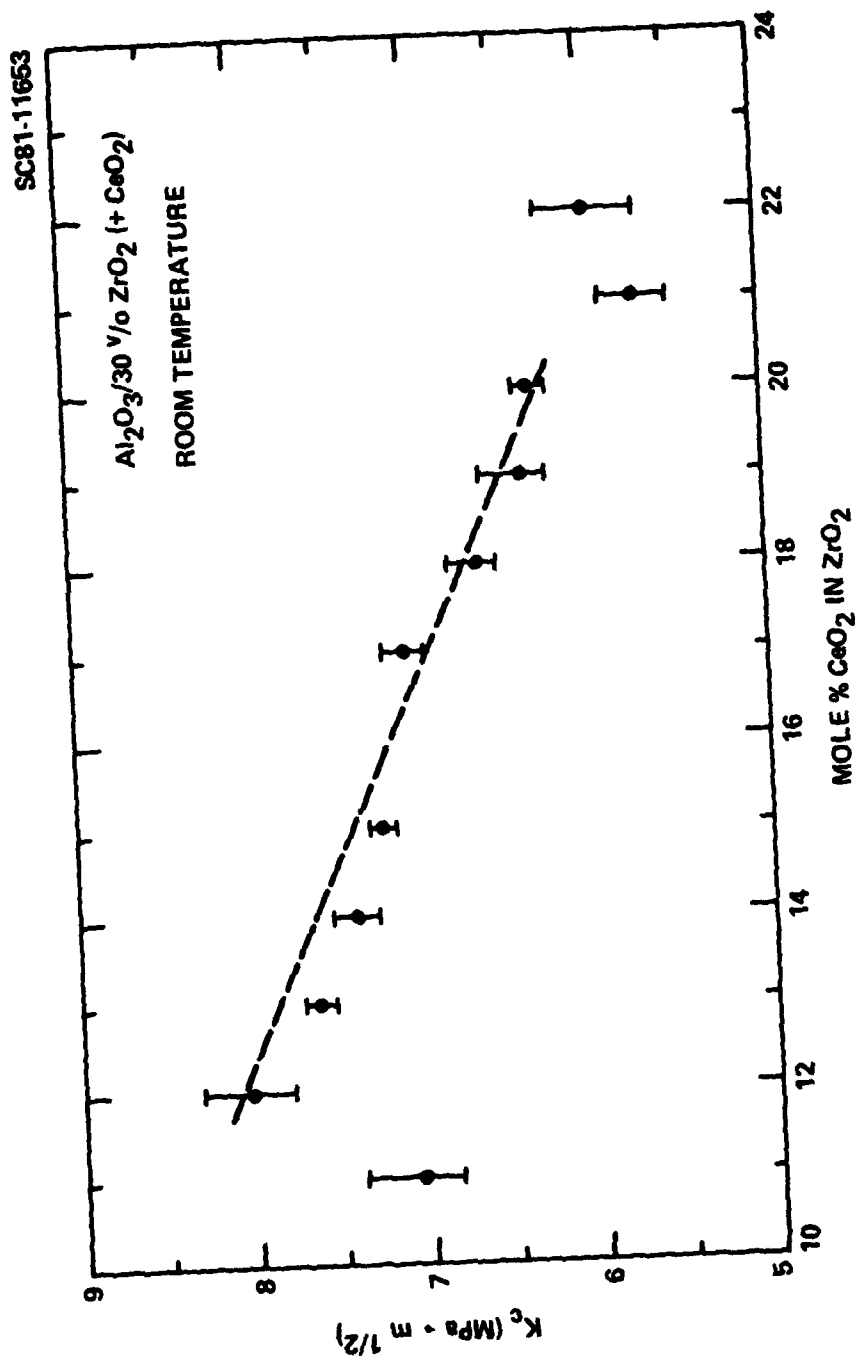MOLE % CeO_2 IN ZrO_2

$K_c (MPa \cdot m^{1/2})$

Fig. 4 Critical stress intensity factor vs mole% CeO_2 at room temperature.

transformation could be expressed as

$$K_c = \left[K_o^2 + \frac{2V_i E_c R(|\Delta G_c| - \Delta U_{se} f)}{(1 - v_c^2)} \right]^{1/2}$$

where K_o is the critical stress intensity factor for the composite without the transformation toughening phenomena, E_c and v_c are the elastic properties of the material, V_i is the volume fraction of the phase which could undergo the stress-induced transformation, R is the size of the transformation zone adjacent to the crack and $(|\Delta G^C| - \Delta U_{se} f)$ is the work loss per unit volume during the stress-induced transformation. Since the magnitude of the chemical free-energy change associated with the transformation, $|\Delta G^C|$, is expected to exhibit the greatest dependence on temperature and alloying relative to the other factors, it was predicted that the contribution of the stress-induced transformation to fracture toughness (i.e., the second term in Eq. (3)) would have the same temperature and alloy dependence as $|\Delta G^C|$. Based on the known temperature and alloying dependence of $|\Delta G^C|$ for the $ZrO_2(t) \rightarrow ZrO_2(m)$ transformation, K_c is expected to decrease with increasing temperature and alloying content which is the general result shown in Figs. 2 and 4, respectively. The following paragraphs present more detailed analysis and discussions of these data with reference to Eq. (3).

4.1   Temperature Dependence

Based on the assumption that $|\Delta G^C|$ is the only temperature dependent factor in Eq. (3), data obtained during this study and reported in Part 4[2] were used to calculate $(|\Delta G^C| - \Delta U_{se} f)$ as a function of temperature for comparison

with the known temperature dependence of $|\Delta G^C|$ for the transformation of pure ZrO_2.[6] This calculation started by determining the size of the transformation zone, R, for each material at room temperature, using the average room temperature value of $(|\Delta G^C| - \Delta U_{se}f)$ calculated in Part 4 for a series of Al_2O_3/ZrO_2 composites, values of K_0 and E_c reported* for each material in Part 4 and room temperature K_c values reported here. Table 2 lists these values and the resulting value of R as determined by rearranging Eq. (3). It should be noted that in Part 2, it was hypothosized that R = the grain size; calculated values of R shown in Table 2 are consistant with the grain sizes of the ZrO_2 phase reported for the hot-pressed materials in Part 4.

In the next step, values of K_c vs temperature reported in Table 1 and the assumed temperature independent values of K_0, E_c, ν_c, V_i and R reported in Table 2 were used to calculate $(\Delta G^C - \Delta U_{se}f)$ as a function of temperature for each material by rearranging Eq. (3). These results are shown in Fig. 5;** Table 2 also reports the slope of each line $(\delta(|\Delta G^C| - \Delta U_{se}f)/\sigma T)$ and the temperature where $(|\Delta G^C| - \Delta U_{se}f) = 0$, (T_0). The fifth line drawn in Fig. 5 is the temperature dependence of $|\Delta G^C|$ for pure ZrO_2 as previously reported by Whitney.[6]

The calculations shown in Fig. 5 contain three results, which adds greater confidence to the validity of the theoretical fracture mechanics calculations (Eq. (3)). First, since $|\Delta G^C|$ is expected to exhibit the greatest temperature dependence relative to other factors in Eq. (3), the slopes of the

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*As in Part 4, ν_c was assumed to be 0.25.
**The four lines coincide at 25°C since it was assumed in step one that all materials had the same value of $(|\Delta G^C| - \Delta U_{se}f)$ at 25°C.

Table 2
Values Used to Analyze K_c vs Temperature Data

Material	K_c^t (MPa·m$^{1/2}$)	K_o^* (MPa·m$^{1/2}$)	$(\Delta G^c - \Delta U_{se}f)^*$ (NJ·m^{-3})	E_c^* (GPa)	v_c^*	v_1	R (µm)	$\dfrac{\partial(|\Delta G^c| - \Delta U_{se}f)}{\partial T}$ (NJ·m^{-3} + C°$^{-1}$)	T_o (C°)
Al$_2$O$_3$/29.3 v/o ZrO$_2$ (+2 m/o Y$_2$O$_3$) (Hot Pressed)	7.45	4.10	188	333	0.25	0.293	0.99	-0.29	690
Al$_2$O$_3$/30 v/o ZrO$_2$ (+2 m/o Y$_2$O$_3$) (Sintered)	8.83	4.10	188	333	0.25	0.30	1.53	-0.27	730
Al$_2$O$_3$/45 v/o ZrO$_2$ (+2 m/o Y$_2$O$_3$) (Hot Pressed)	8.30	3.70	188	285	0.25	0.45	1.10	-0.21	900
ZrO$_2$ (+2 m/o Y$_2$O$_3$) (Hot Pressed)	6.71	3.90	188	207	0.25	1.00	0.36	-0.24	830
Average of four materials								-0.25	785
ZrO$_2$ (pure)[6]								-0.25	1200
Zr$_{0.96}$Y$_{0.04}$O$_{1.98}$ (ZrO$_2$ + 2 m/o 1/2 O$_3$)[7,8]									500 - 630°C

†Room temperature values, Table 1
*Room temperature values, Part 4.

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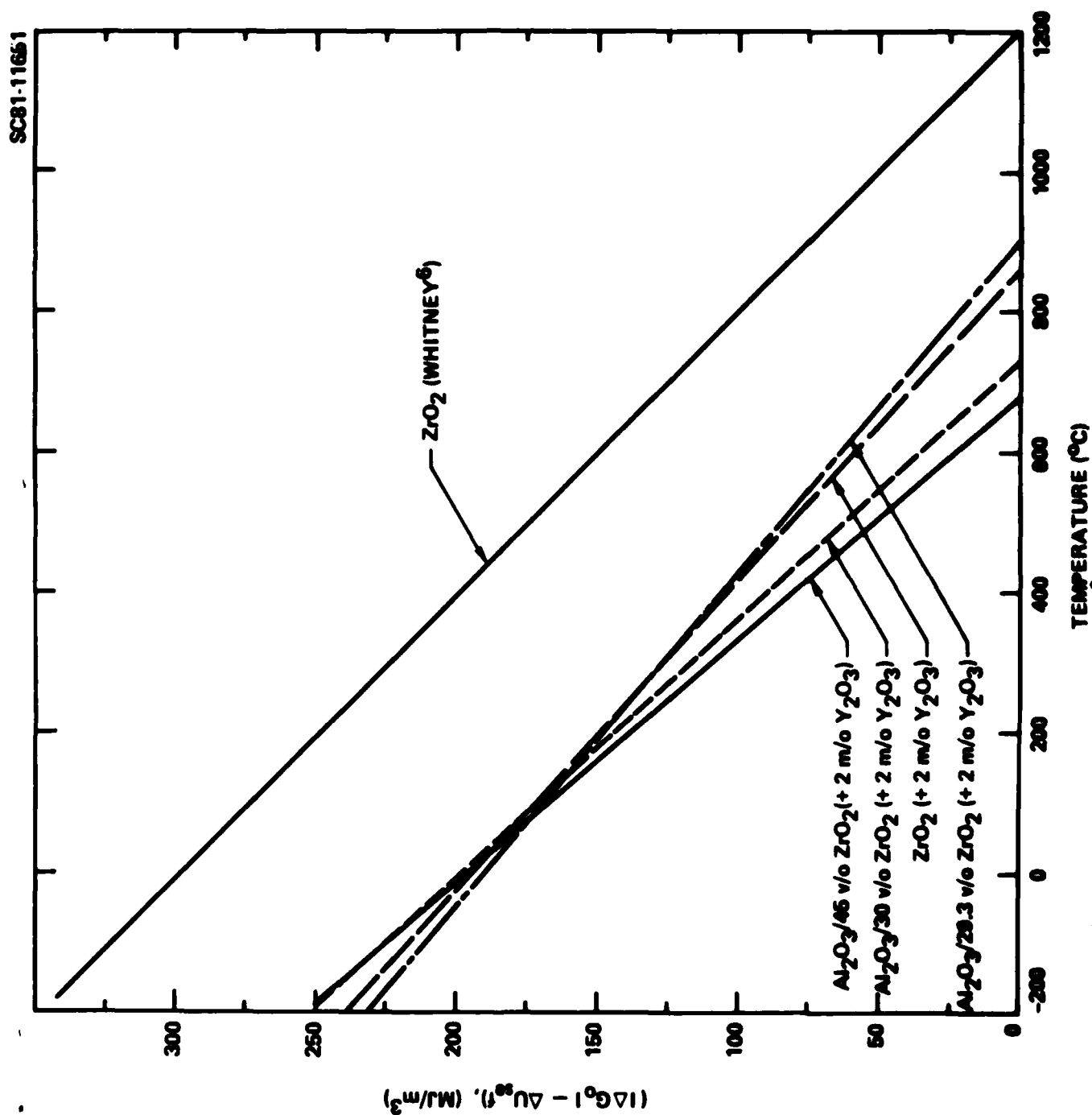
Fig. 5 Calculated values of $(|\Delta G_c^f| - \Delta U_{se}^f)$ vs temperature for four materials studied. Upper line is $|\Delta G_c^f|$ vs temperature for pure ZrO_2 as

four lines in Fig. 5 should be the same as $\delta|\Delta G^C|/\delta T$ for $Zr_{0.96}Y_{0.04}O_{1.98}$ (ZrO_2
+ 2 m/o Y_2O_3). Although $|\Delta G^C|$ vs temperature data do not exist for this solid-
solution compound, it is important to note that the slopes are nearly coincident
(see Table 2) for that of pure ZrO_2 as reported by Whitney.[6] Second, the
temperature (T_0) where ($|\Delta G^C| - \Delta U_{se}f$) = 0 lie within the range of
transformation temperatures (where ΔG^C = 0) (see Table 2) for $Zr_{0.96}Y_{0.04}O_{1.98}$
powder.[7,8] This result suggests that the residual strain energy associated with
the ZrO_2 grains that contribute most to the fracture toughness is very small,
viz. $\Delta U_{se}f$ = 0. Third, the slope of the lines in Fig. 5 critically depend on
the value of R chosen, i.e., larger or smaller values of R would not have
resulted in the good agreement with $\delta|\Delta G^C|/\delta T$ for pure ZrO_2. Values of R
calculated from room temperature data* (Step 1) not only result in reasonable
slopes for $\delta|\Delta G^C|/\delta T$, but they are also in good agreement with the size of the
ZrO_2 grains as hypothesized by theory.

4.2   Effect of Alloying

Based on the assumption that $|\Delta G^C|$ is the only factor in Eq. (3)
affected by alloying CeO_2 with ZrO_2, the K_c results presented in Eq. (2) have
been used to calculate the combined factor ($|\Delta G^C| - \Delta U_{se}f$)R. The linear
expression resulting from combining Eq. (2) and (3) with the appropriate values[2]

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*A second approach can also be used to determine R for each material by
calculating the combined product R($|\Delta G^C| - \Delta U_{se}f$) in Eq. (3) as a
function of temperature and assuming that $\delta(|\Delta G^C| - \Delta U_{se}f)/\delta T$ = 0.248
$MJ \cdot m^{-3} \cdot C^{\circ -1}$ (the value of $\delta|G_c|/\delta T$ for pure ZrO_2).[6] Using this approach,
values of R for the four materials listed in Table 2 are 1.2 μm, 1.65 μm,
0.95 μm and 0.34 μm, respectively.

$K_0 = 4.1$ MPa m$^{1/2}$, $E_0 = 333$ GPa, $\nu_c = 0.25$ and $V_i = 0.30$ for the Al$_2$O$_3$/30 v/o ZrO$_2$ (+ CeO$_2$) compositions is

$$(|\Delta G^C| - \Delta U_{se}f)R = (415 - 15.8 \text{ M}) \text{ MJ/m}^2 \quad . \qquad . \qquad (4)$$

Equation (4) can be used to estimate two thermodynamic properties of ZrO$_2$, which again adds greater confidence to the fracture mechanisms theory as expressed in Eq. (3). First, by extrapolating the data obtained between M = 12 to 20 m/o CeO$_2$ to M = 0, one obtains the value of $(|\Delta G^C| - \Delta U_{se}f)R = 415$ MJ/m^2 for pure ZrO$_2$. By chosing R = 1.5 μm, the value determined to be consistent with the K$_c$ vs temperature data for a similar, sintered Al$_2$O$_3$/30 v/o ZrO$_2$ composite discussed in the last section, one obtains $(|\Delta G^C| - \Delta U_{se}f) = 275$ MJ/m^3. It is interesting to note that this value agrees almost exactly with the room temperature value of $|\Delta G^C| = 290$ MJ/m^3 for pure ZrO$_2$ as previously calculated by Whitney (see Fig. 5). Although this near perfect agreement may be fortuitous, it again suggests that the residual strain energy ($\Delta U_{se}f$) associated with the transformed grains adjacent to the crack surfaces can be neglected in estimating their contribution to fracture toughness.

Second, previous phase equilibria work[5] in the ZrO$_2$-CeO$_2$ binary system has suggested that CeO$_2$ additions in the range between 15 to 20 m/o CeO$_2$ lowers the tetragonal → monoclinic transformation temperature below 25°C. K$_c$ measurements (see Fig. 2) clearly show that the tetragonal phase contributes to toughening over the complete range of CeO$_2$ studied (11 m/o to 22 m/o). That is, K$_c$ measurements strongly suggest that the eutectoid temperature is > 25°C. Using the fracture mechanics data, one can estimate the eutectoid temperature by

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assuming that $\Delta U_{se}f = 0$ and determing the value of M in Eq. (4) where $|\Delta G^{C}|R = 0$. This condition exists when M = 26 m/o CeO_2. By constructing a line between 1200°C and 26 m/o CeO_2 on the ZrO_2-CeO_2 phase diagram and recognizing that the tetragonal + cubic phase field exists when M > 20 m/o CeO_2, one estimates the eutectoid temperature as 270°C which alters the phase diagram shown in Fig. 1 to that shown in Fig. 6.

5.0 CONCLUSIONS

1. The fracture toughness of materials containing tetragonal ZrO_2 decreased with increasing temperature and alloying addition, consistent with theoretical predictions.

2. An analysis of the data suggests that the residual strain energy associated with the transformed ZrO_2 gains can be neglected. Thus, the equation which appears to explain the contribution of the stress-induced phase transformation to fracture toughness can be rewritten as

$$K_c = \left[K_o^2 + \frac{2|\Delta G_c|E_c V_1 R}{(1 - v_c^2)} \right]^{1/2} . \tag{5}$$

3. The fracture mechanics data, when analyzed with respect to theory as expressed by Eq. (3), best fit the thermodynamic data for ZrO_2 when it was assumed that the size of the transformation zone is the same size as the ZrO_2 grains.
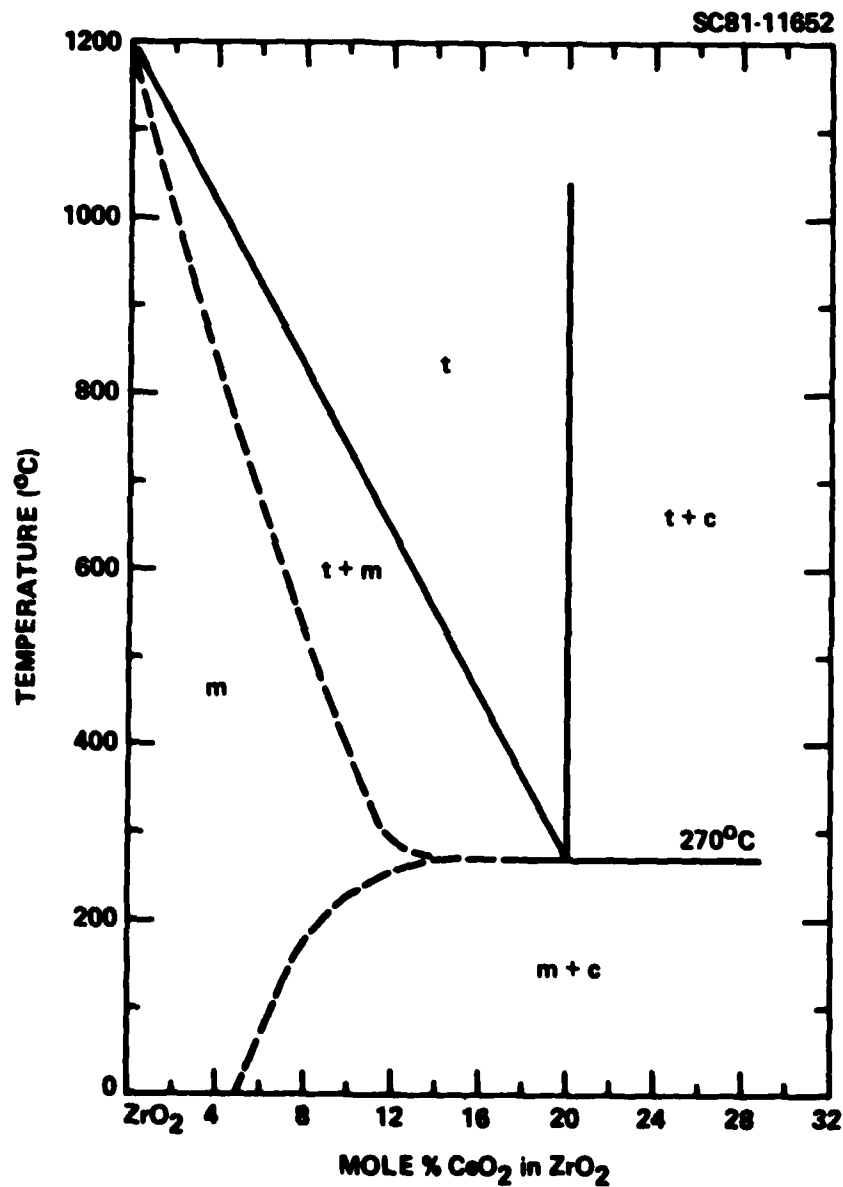
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Fig. 6 A portion of the ZrO_2-CeO_2 phase diagram, in which the eutectoid temperature has been estimated through fracture mechanics data.

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